



An application of multiple regression for predicting turbidity of standard water quality for industrial and household consumption

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ARTICLE INFO

Received: 15 September 2021

Revision: 14 Oktober 2021

Accepted: 16 Oktober 2021

Keywords:

Water Quality

Turbidity

Multiple regression

ABSTRACT

A multiple regression approach was applied in this study with the aim of predicting Turbidity value of standard water in water treatment plant. Turbidity is a level of cloudiness in water due to the presence of particles or microorganisms. Turbidity in standard water did not affect human health in term of hazardous, even though it represent of poor quality water. Water treatment plant reduce the cloudiness in water by applying chlorination process. There are three independent variables of water quality involved to predict turbidity value. They are PH, color-spectrum and electrical conductivity. The correlation among variables were checked before conducting multiple regression. Color-spectrum has the highest correlation with the turbidity. The stepwise approach remain two independent variables involved in multiple regression equation, color-spectrum and electrical conductivity with the value of R-square equal to 0,97. Meaning that the two variables has the ability of explaining variances in turbidity up to 97 %.

1. INTRODUCTION

Water supply has important roles in human life either for personal purpose or for business activities. The standard water require special treatment before distributed into residential and industrial area. According to physical characteristic, standard water has several index set by the ministry of industry such as turbidity, color spectrum, electrical conductivity. Turbidity is defined as the "optical quality [of water] that causes light to be scattered and absorbed rather than transmitted in straight lines through a sample" [1, 2, 3]. Turbidity is used to indicate water quality [4, 5, 6, 7] and it is an important parameter to measure the water quality [8]. The aim of the research is to predict the turbidity of standard water in a water treatment plant using a multiple regression approach. Linear models have been used to predict water quality parameters which have provided useful insights into the behaviour of a natural system, however, have demonstrated relatively modest results [1].

2. LITERATURE REVIEW

Turbidity is a parameter for represent water quality. Turbidity is a term used to describe the clearness of a water decreases due to the presence of smallest substances, particles or microorganisms [9, 10, 11]. Refer to the World Health Organisation (WHO). The turbidity level of the water before the chlorination process is not more than 1 Nephelometric Turbidity Unit (NTU). The score of turbidity in raw water is very influential in determining the dosage of chemical raw materials (operating supplies) to be used in water treatment plant [12]. There are various studies focus on turbidity as one parameters of water quality [1], [2], [13, 14, 15]. The highest turbidity score in the water meaning that its quality is low.

Turbidity of water could be caused by the existence of other suspended particles, such clay and silts [16], or soluble colored organic compounds, and plankton and other microscopic organisms [17]. According to Mandal [17], various studies exclaimed that pH on the water system found to be significant showing positive and negative correlation on turbidity removal. The summary



of previous research that focus on several parameter of water quality is presented in Table 1.

Table 1. Previous study related on water quality parameters

| Quality water parameters | Authors (years) | Methods | Finding |
|--------------------------|---------------------------------------|------------------------------|--|
| Turbidity | LeChevallier et al. (1981) [16] | Linear Regression | Turbidity has a significant effect on water quality |
| | Mustapha and Abdu (2012) [15] | Principal component analysis | |
| | Stevenson et al (2019) [1] | Multiple Linear regression | |
| | Song and Zhang (2020) [4] | Generelised Linear Model | |
| | | Random Forest | |
| pH | Mandal, H. E (2015) [17] | Neural Network | no direct influence of wastewater pH on turbidity |
| | | Experimental Design | |
| Spectral | Read et al (2015) [18] | Geospatial Technique | attempt to develop spectral library for water quality parameters and its application in spectral similarity analysis |
| | V. Garg et al. (2017) [19] | | |
| Conductivity | Najah et al (2009) [20] | Artificial Neural Network | revealed the usefulness of sensor and real-time recording technooogy over traditional water sampling and laboratory analysis |
| | Read et al (2015) | Random Forest | |
| | E. Skarbøvik and R. Roseth (2015) [8] | Sensor | |
| | | | |

3. RESEARCH METHOD

3.1 Data

Data in this research were collected from water treatment plant located in Banten Province, Indonesia. As much of 187 samples were taken for conducting multiple linear model. The samples are measured for four parameters which are turbidity, pH, color and electrical conductivity.

3.2. Descriptive statistics

Descriptive statistics of the water quality parameters have been summarized in Table 2. Table 2 describes statistical descriptive of parameters in this study. The pH mean is 7.6. it is explained clearly that the standard water in the water treatment plant is which is slightly above neutral level. However, far from acidity or alkalinity.

3.3. Correlation

It is required to check the correlation lying in between the parameters involved in this study. From Table 2, we can identify that Spectral has the strongest relation with Turbidity among other parameters.

Table 2. Statistical descriptive of parameters

| Statistics | Turbidity | Spectro | DHL | pH |
|--------------------------|-----------|---------|--------|---------|
| Mean | 63,87 | 583,29 | 172,27 | 7,63 |
| Std. Error | 1,79 | 17,16 | 2,01 | 0,01 |
| Median | 56,9 | 515,5 | 169 | 7,63 |
| Mode | 49,2 | 450 | 209 | 7,61 |
| Std. Dev | 24,47 | 234,08 | 27,45 | 0,15 |
| Variance | 598,82 | 54793,7 | 753,69 | 0,02 |
| Kurtosis | 4,45 | 6,82 | -0,84 | 0,03 |
| Skewness | 1,73 | 2,09 | 0,10 | -0,19 |
| Range | 154,5 | 1712 | 118 | 0,79 |
| Minimum | 32,5 | 199 | 113 | 7,25 |
| Maximum | 187 | 1911 | 231 | 8,04 |
| Sum | 11880 | 108490 | 32043 | 1419,94 |
| Count | 186 | 186 | 186 | 186 |
| Confidence Level (95,0%) | 3,54 | 33,86 | 3,97 | 0,02 |

In the second row, with the correlation value of -0.515 electrical conductive has medium -relation to the turbidity with a different direction. Since the correlation has a minus sign. If the electrical conductivity value is increased, the Turbidity level is low.

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3.4. Multiple linear regression

Multiple linear regression is a statistical tool to analyze interrelationship between dependent variable with two or more independent variables. Mathematical model represent multiple linear regression is shown in equation (1) refer to the similar model in [8]

$$y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \dots + \beta_nx_n + \varepsilon \quad (1)$$

where

y = Dependent variable (Turbidity in this case)

x_n = independent variable (parameters of water quality, $n = 1...3$)

β_0 = regression coefficient

ε = random error in term of regression model

By applying data analysis of 187 data, we can calculate the regression statistics as summarized in Table 4. Multiple R describes the correlation between actual and predicted values of the dependent variable; in this study refer to Turbidity. The R-square is the model's accuracy in explaining the dependent variable. Table 5 shows the result of ANOVA test for regression. The significance of F felt far below the F statistic with degree of freedom of 2. Meaning that, the multiple regression model developed is adequate for prediction turbidity purpose.

Table 3. Correlation matrix among variables

| | Turbidity | Spectro | DHL | pH |
|-----------|-----------|---------|-------|----|
| Turbidity | 1 | | | |
| Spectro | 0.984 | 1 | | |
| DHL | -0.515 | -0.471 | 1 | |
| pH | -0.212 | -0.239 | 0.148 | 1 |

Table 4. Regression statistics of the water quality parameters for 187 observations

| | |
|-------------------|----------|
| Multiple R | 0,985525 |
| R Square | 0,971259 |
| Adjusted R Square | 0,970947 |
| Standard Error | 4,16417 |

Table 5. ANOVA for regression

| | df | SS | MS | F | Sig. F |
|------------|-----|--------|-------|---------|----------|
| Regression | 2 | 107822 | 53911 | 3109,01 | 1,5E-142 |
| Residual | 184 | 3190 | 17,34 | | |
| Total | 186 | 111013 | | | |

Table 6. p-value of coefficient regression for independent variables

| | Coefficients | P-value |
|-------------------------|--------------|-----------|
| Intercept | 15,91223 | 1,846E-08 |
| color spectral | 0,09962 | 1,81E-131 |
| electrical conductivity | -0,0588 | 5,569E-06 |

Table 6 describes the coefficient of variables in multiple regression model. The p-value of each variable is consider significant for using in the multiple regression model developed since the value below 0.05.

4. RESULT AND DISCUSSION

This study attempt to predict the standard water quality through the interrelationship among turbidity as the dependent variables, with three independent variables such as pH, Spectral and electrical conductivity. A multiple regression model was employed to find the mathematical model to predict turbidity level. Table 7 in the previous section shows the p-value for each coefficient of spectral (x1) and electrical conductivity (x2) are significant. Therefore, Turbidity level could be predicted by applying the equation below.

$$y = 15.92 + 0.0996 x_1 - 0.05889 x_2 + \epsilon \quad (2)$$

The multiple regression above is quite robust since the R square is 0.971259. Meaning that spectral (x1) and electrical conductivity (x2) can explained the variation of turbidity up to 97.13%, and the rest variation is explained by others. See Fig, 1 for the plot. In order to check that the assumption of multiple regression model are fulfilled, we plot the residual value. Figure 2 shows the residual plot of color spectral of standard quality water.

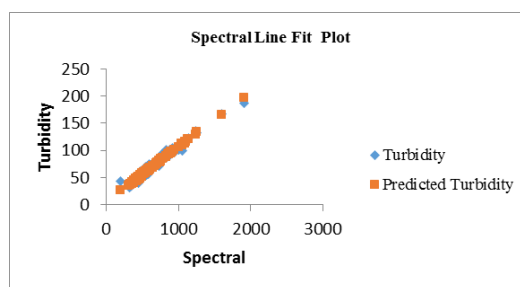


Figure 1. Turbidity vs predicted one

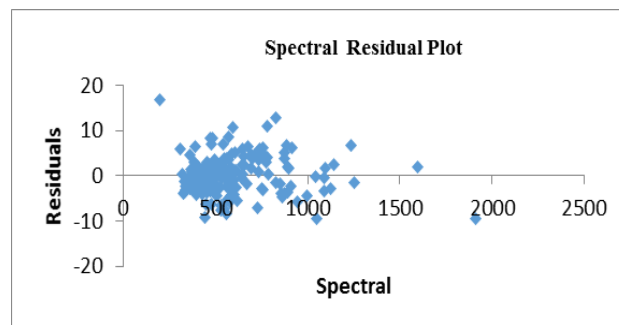


Figure 2. Spectral Residual Plot fulfill the assumption

5. CONCLUSION

This study has developed a turbidity prediction model by applying a multiple regression method with a stepwise approach. This model is very useful for managing water treatment plant. The level of turbidity has impact on purchasing the chemical stuff for improved the water quality.

ACKNOWLEDGEMENT

The authors would like to acknowledge the generous support from the Indonesia Endowment Fund for Education (LPDP); Industrial Engineering University of Pelita Harapan

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